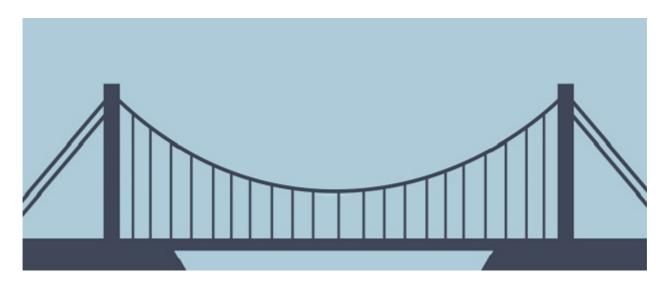


The Bridge to A level PiXL Y11 Maths Bridging Unit



This pack contains a programme of activities and resources to prepare you to start A-level in Maths in September.

It is aimed to be used after you complete your GCSE throughout the remainder of the summer term and over the summer holidays to ensure you are ready to start your course in September.

The resources include:

- 1. Links to websites where you can research the topics you will be exploring in your sixth form courses and get a flavour of mathematics beyond GCSE.
- 2. 15 key pre-knowledge topics that will help you to be successful in your course. The topics covered are a mixture of GCSE topics, and topics which extend GCSE but which will be very useful on your A level course.
- 3. A diagnostic assessment that will test your key knowledge of these 15 topics.
- 4. Suggested therapies to help you with those topics with which you are having difficulty.
- 5. A second assessment which will test the effectiveness of your use of the therapies.
- 6. A bank of problem solving questions to accompany each of the 15 topics to test that you can apply the skills that you have learned.



Websites

NRich

http://nrich.maths.org/secondary-upper

Mathwire

http://mathwire.com/archives/enrichment.html

The History of Maths – Wikipedia

https://en.wikipedia.org/wiki/History_of_mathematics

The History of Maths – Youtube video

https://www.youtube.com/watch?v=cy-8IPVKLlo

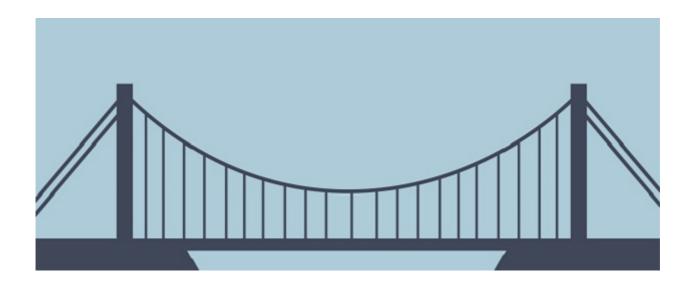
15 key Topics

1	Solving quadratic equations
2	Changing the subject
3	Simultaneous equations
4	Surds
5	Indices
6	Properties of Lines
7	Sketching curves
3	Transformation of functions
Э	Pythagoras' theorem and Trigonometric ratios
10	Sine / Cosine Rule
11	Inequalities
12	Proof
13	Vectors
14	Probability
15	Statistics



The Bridge to A level

Diagnosis





1 <u>Solving quadratic equations</u>

Question 1

Solve $x^2 + 6x + 8 = 0$

(2)

Question 2

Solve the equation $y^2 - 7y + 12 = 0$

Hence solve the equation $x^4 - 7x^2 + 12 = 0$

(4)

Question 3

(i) Express $x^2 - 6x + 2$ in the form $(x-a)^2 - b$

(3)

(ii) State the coordinates of the minimum value on the graph of $y = x^2 - 6x + 2$

(1)



2 <u>Changing the subject</u>

Question 1

Make v the subject of the formula $E = \frac{1}{2} mv^2$

(3)

Question 2

Make r the subject of the formula V = $\frac{4}{3} \Pi r^2$

(3)

Question 3

Make c the subject of the formula $P = \frac{C}{C+4}$

(4)



3 <u>Simultaneous equations</u>

Question 1

Find the coordinates of the point of intersection of the lines y = 3x + 1 and x + 3y = 6

(3)

Question 2

Find the coordinates of the point of intersection of the lines 5x + 2y = 20 and y = 5 - x

(3)

Question 3

Solve the simultaneous equations

$$x^2 + y^2 = 5$$

$$y = 3x + 1$$

(4)



4 <u>Surds</u>

Question 1

(i) Simplify $(3 + \sqrt{2})(3 - \sqrt{2})$

(2)

(ii) Express $\frac{1+\sqrt{2}}{3-\sqrt{2}}$ in the form $a+b\sqrt{2}$ where a and b are rational

(3)

Question 2

(i) Simplify $5\sqrt{8}+4\sqrt{50}$. Express your answer in the form $a\sqrt{b}$ where a and b are integers and b is as small as possible.

(2)

(ii) Express $\frac{\sqrt{3}}{6-\sqrt{3}}$ in the form $p+q\sqrt{3}$ where p and q are rational

(3)



5 <u>Indices</u>

Question 1

Simplify the following

- (i) a⁰
- (ii) $a^6 \div a^{-2}$
- (iii) (9a⁶b²)^{-0.5}
- Question 2
- (i) Find the value of $\left(\frac{1}{25}\right)^{-0.5}$
- (ii) Simplify $\frac{(2x^2y^3z)^5}{4y^2z}$
- Total / 10

(1)

(3)

(2)

(3)



(5)

6 <u>Properties of Lines</u>

	<u> ,</u>	
Ques	tion 1	
A (0,2	2), B (7,9) and C (6,10) are three points.	
(i)	Show that AB and BC are perpendicular	
		(2
(ii)	Find the length of AC	(3
		(2
Ques	tion 2	
Find,	in the form $y = mx + c$, the equation of the line passing through A (3,7) and B (5,-1).	
Show	that the midpoint of AB lies on the line $x + 2y = 10$	



7 Sketching curves

Question 1

In the cubic polynomial f(x), the coefficient of x^3 is 1. The roots of f(x) = 0 are -1, 2 and 5.

Sketch the graph of y = f(x)

(3)

Question 2

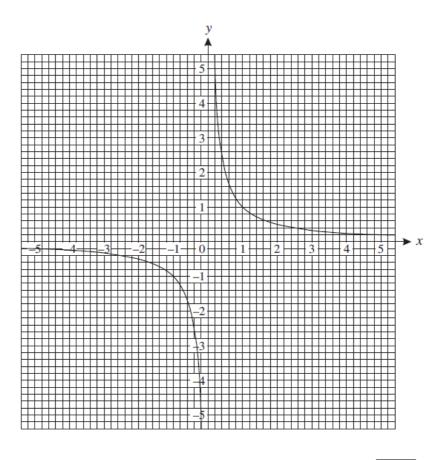
Sketch the graph of $y = 9 - x^2$

(3)

Question 3

The graph below shows the graph of $y = \frac{1}{x}$

On the same axes plot the graph of $y = x^2 - 5x + 5$ for $0 \le x \le 5$



(4)



Transformation of functions 8

Question 1

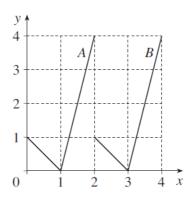
The curve $y = x^2 - 4$ is translated by $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$

Write down an equation for the translated curve. You need not simplify your answer.

(2)

Question 2

This diagram shows graphs A and B.



(i) State the transformation which maps graph A onto graph B

(2)

The equation of graph A is y = f(x). (ii)

Which one of the following is the equation of graph B?

$$v = f(x) + 2$$

$$y = f(x) + 2$$
 $y = f(x) - 2$ $y = f(x+2)$

$$y = f(x+2)$$

$$y = f(x-2)$$

$$y = 2f(x)$$

$$y = f(x+3)$$
 $y = f(x-3)$

$$y = f(y_3)$$

$$y = 3f(x)$$

Question 3

Describe the transformation which maps the curve $y = x^2$ onto the curve $y = (x+4)^2$ (i)

(2)

(2)

Sketch the graph of $y = x^2 - 4$ (ii)

(2)



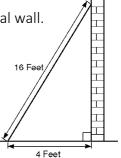
9 Trigonometric ratios

Question 1

Sidney places the foot of his ladder on horizontal ground and the top against a vertical wall.

The ladder is 16 feet long.

The foot of the ladder is 4 feet from the base of the wall.



- (i) Work out how high up the wall the ladder reaches. Give your answer to 3 significant figures.
- (ii) Work out the angle the base of the ladder makes with the ground. Give your answer to 3 significant figures

(2)

Question 2

Given that $\cos \Theta = \frac{1}{3}$ and Θ is acute, find the exact value of $\tan \Theta$

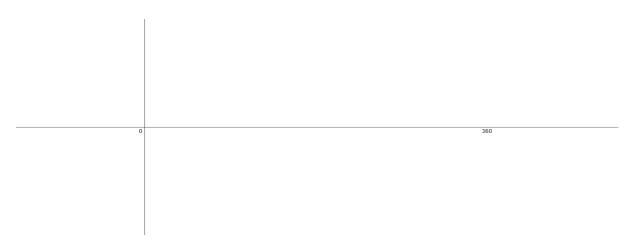
(3)

(3)

(2)

Question 3

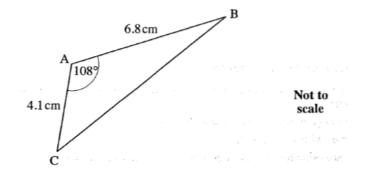
Sketch the graph of $y = \cos x$ for $0 \le x \le 360^{\circ}$





10 Sine / Cosine Rule

Question 1



For triangle ABC, calculate

(i) the length of BC

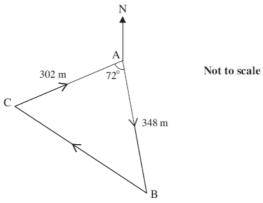
(ii) the area of triangle ABC

(3)

(3)

Question 2

The course for a yacht race is a triangle as shown in the diagram below. The yachts start at A, then travel to B, then to C and finally back to A.



Calculate the total length of the course for this race.

(4)



(3)

11 <u>Inequalities</u>

Question 1

Solve

- a) $x^2 36 \le 0$
- b) $9x^2 25 \ge 0$
- c) $3x^2 + 10x < 0$

Question 2

Solve $\frac{21}{x+2} - \frac{5}{x+1} < 4$

.....(4)

Question 3

Solve $3x^2 - 8 > 2x$

.....(3)



12 <u>Algebraic proof</u>

Question 1

a) If n is a positive integer, write down expressions for the next two consecutive integers.

(1)

b) Use algebra to prove that the sum of three positive consecutive integers is always a multiple of 3.

(3)

Question 2

Prove that the square of an odd number is also odd.

(3)

Question 3

Given that x is a positive integer, prove that $\frac{4x^3+20x}{2x^2+10}$ is always even.

(3)



13 <u>Vectors</u>

Question 1

OAP is a triangle

$$\overrightarrow{OA} = 2\mathbf{f} + \mathbf{g}$$
 and $\overrightarrow{OB} = 3\mathbf{h}$
P is the point on AB such that AP: PB = 2:1

(a) Find the vector BA in terms of **f**, **g** and **h**.

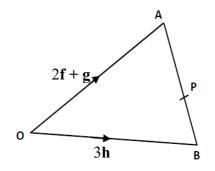


Diagram NOT drawn accurately

.....(1)

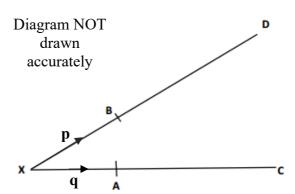
(b) Find the vector PO in terms of **f**, **g** and **h**

(2)

Question 2

B is the point on AD such that XB:BD is 1:2 A is the point on XC such that XA:XC is 1:2

$$\overrightarrow{XB} = \mathbf{p} \text{ and } \overrightarrow{XA} = \mathbf{q}$$



Use vectors to explain the geometrical relationships between the line segments BA and DC.

(4)

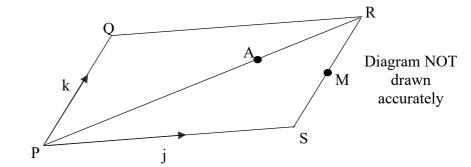


Question 3

PQRS is a parallelogram.

A is the point on PR such that PA:AR is 2:1 M is the midpoint of RS.

(b) Prove that Q, A and M are co-linear.



(3)



14 <u>Probability</u>

Question 1

Question 1	
A box contains 3 new batteries, 5 partly used batteries and 4 dead batteries.	
Kelly takes two batteries at random.	
Work out the probability that she picks two different types of batteries.	
	(3)
Question 2	
Question 2	
Caleb either walks to school or travels by bus.	
The probability that he walks to school is 0.75.	
If he walks to school, the probability that he will be late is 0.3.	
If he travels to school by bus, the probability that he will be late is 0.1.	
Work out the probability that he will not be late.	
	(3)



Question 3

The two way table shows the number of deaths and serious injuries caused by road traffic accidents in Great Britain in 2013.

		Speed Limit					
		20 mph	30 mph	40 mph	Total		
	Fatal	6	520	155	681		
Type of Injury	Serious	420	11582	1662	13664		
	Total	426	12102	1817	14345		

Vork out

an e	estimate for the probability:	
(a)	that the accident is serious.	
(b)	that the accident is fatal given that the speed limit is 30 mph.	(1
(0)	that the accident is ratal given that the speed limit is 50 mph.	
(c)	that the accident happens at 20 mph given that the accident is seriou	(1
` '		
		(2
	Total / 10	

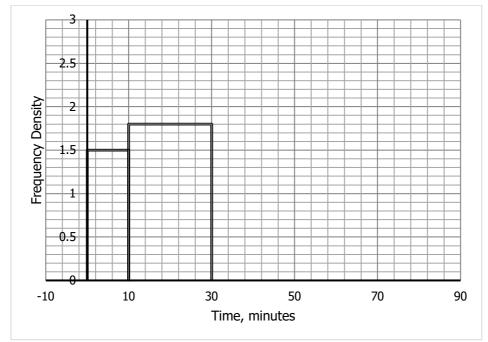


15 <u>Statistics</u>

Question 1

The histogram and the frequency table show some information about how much time vehicles spent in a car park.

Т	ime, mir	Frequency	
0	< x ≤	10	
10	< x <	30	
30	< x <	60	75
60	< x ≤	80	24
		Total	150



a) Use the information to complete the histogram

b) Use the histogram to find the missing frequencies in the table

.....

(2)

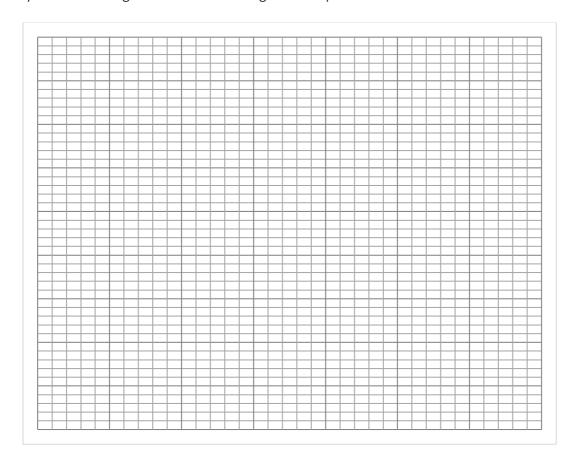
(2)



The table shows the length of 678 phone calls made at a call centre

	Time, se	Frequency	
0	< x ≤	20	20
20	< x ≤	60	148
60	< x ≤	120	240
120	< x ≤	300	270
		Total	678

a) Draw a fully labelled histogram to show the length of the phone calls.



b) Estimate the number of phone calls that lasted more than 4 minutes.

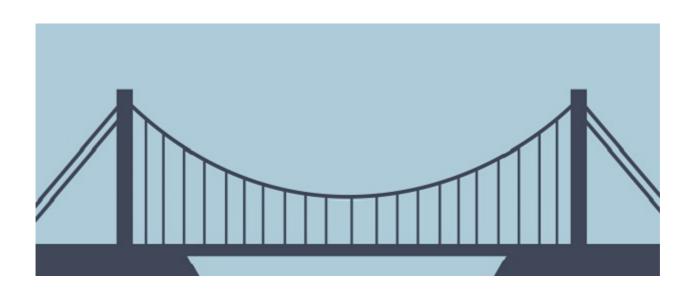


(4)



The Bridge to A level

Diagnosis Mark Scheme





Section	Question	Answer	Marks	Notes
1	1	-2, -4	M1	$(x \pm 2)(x \pm 4)$
			A1	
	2	y = 3 or y = 4 cao	M1	For (y-3)(y+4) oe eg use of quad form
			A1	y = 3 or y = 4 cao
		$x = \pm \sqrt{3}$ or $x = \pm 2$ cao	B2	B1 for two roots correct or ft 'their' y
				B2 for cao
	3(i)	$(x-3)^2-7$	B1	$(x-3)^2$
			M1A1	-7
	3(ii)	(3,-7)	B1	ft from part (i)
2	1	$V = \sqrt{\frac{2E}{m}}$ cao www	В3	Award M1 for a correct first constructive
		$\sqrt{-\sqrt{m}}$ Cao www		step, M2 for $v^2 = \frac{2E}{m}$ oe
	2	3 3V	В3	step, M2 for $v^2 = \frac{2E}{m}$ oe Award M2 for $r^3 = \frac{3V}{4\Pi}$, M1 for cube root
		$r = \sqrt[3]{\frac{3V}{4\Pi}}$		of 'their' r³
	3	$C = \frac{4P}{1-P}$ oe	M1	PC + 4P = C
		1-P	M1	4P = C - PC
			M1	4P = C(1 - P)
			A1	, ,
3	1	(0.3,1.9)	M1	for substitution or for rearrangement
			A1A1	one mark each coordinate
	2	$(\frac{10}{3}, \frac{5}{3})$	M1	for substitution or for rearrangement
		3 3	A1A1	one mark each coordinate
				Note: award B2 if roiunded to 1dp or
				worse
	3	$(\frac{2}{5}, \frac{11}{5})$ or (-1,-2) or answer	M1	substituting linear into non-linear
		given as x=, y=	M1	forming quadratic in x
			A1A1	one mark for each set of solutions
	4/:)			
4	1(i)	7	M1	9-2
	1/::)	5 4 —	A1	
	1(ii)	$\frac{5}{7} + \frac{4}{7}\sqrt{2}$	M1	multiplying top and bottom by $3 + \sqrt{2}$
			M1	$\frac{3+2+3\sqrt{2}+\sqrt{2}}{7}$ if one (or none) error only
	2/;)	2012	A1	·
	2(i)	30√2	M1 A1	for $\sqrt{8} = 2\sqrt{2}$ or $\sqrt{50} = 5\sqrt{2}$
	2/ii\	1 2 /2	M1	
	2(ii)	$\frac{1}{11} + \frac{2}{11}\sqrt{3}$	M1	multiplying top and bottom by $6 + \sqrt{3}$
			A1	denominator = 11 (or 33)
			AT	



	ı		1	Partners in excellence
5	1(i)	1	B1	
	1(ii)	a ⁸	B1	
	1(iii)	1	B1	3b
		$\overline{3a^3b}$	B1	a ³
			B1	inverse
	2(i)	±5	M1	for $\sqrt{25}$ or $\frac{1}{5}$ seen
			A1	5
	2(ii)	$8x^{10}y^{13}z^4$ (or $2^3x^{10}y^{13}z^4$)	В3	B2 for 3 elements correct
				B1 for 2 elements correct
6	1(i)	Grad AB = 1	M1	
		Grad BC = -1	M1	
		product of gradients = -1 hence	C1	
		perp		
	1(ii)	10	M1	Use of pythagoras
			A1	
	2	y = -4x + 19 cao	M1	calculating m
			M1	using $(y - 7) = m(x-3)$
			A1	
		Midpoint (4,3)	B1	
		verifying on line x + 2y = 10	C1	
7	1	Cubic the correct way up	G1	
		-1, 2 and 5 indicated on x-axis	G1	
		10 indicated on y-axis	G1	
	2	Negative quadratic curve	G1	
		Intercept (0,9)	G1	
		Through (3,0) and (-3,0)	G1	
	3	Any correct y value calculated	B1	
		(0,5), (1,1), (2,-1), (3,-1), (4,1)	B1	
		and (5,5) calculated		
		Above points plotted	G1	
		Smooth parabola through the	G1	
		points		
8	1	$y = (x-2)^2 - 4$	B2	M1 if y omitted, or for y = $(x + 2)^2 - 4$
	2(i)	Translation of	B1	
		$\binom{2}{0}$	B1	
		0		
	2(ii)	y = f(x - 2)	B2	B1 for y = f(x+2)
	3(i)	Translation of	B1	
		$\begin{pmatrix} -4 \\ 0 \end{pmatrix}$	B1	
	3(ii)	sketch of parabola right way up	B1	
		min at (0,-4) and graph through	B1	
		(-2,0) and (2,0)		
		(-,-)		



				Partners in excellence
9	1(i)	15.5	M1	Use of Pythagoras
	- (11)		A1	4
	1(ii)	x = 75.5°	M1	$(\cos x = \frac{4}{16})$ correct ratio and substitution
			A1	16'
	2	√8 or 2√2 (but not ± √8)	M1	Use iof pythagoras
			M1	use of tan Θ = opp / adj
			A1	
	3	Smooth curve between y = 1	G1	
		and y = -1		
		(90,0) and (270,0)	G1	
		(0,1), (180,-1), (360,1)	G1	
		(5,1), (155, 1), (555,1)	0 =	
10	1(i)	9.0 or 8.96 or 8.960	M1	for use of cosine rule
			M1	for square-rooting 'their' 80.2(8)
			A1	
	1(ii)	13.3 or better (13.2577)	M1	use of 'their' 0.5 x 4.1 x 6.6 x sin 108
	1 -(11)	13.3 of better (13.2377)	A1	correct values
		DC 204/ L	A1	ans
	2	BC = 384 (or better)	M1	recognisable attempt at cosine rule
			M1	$BC^2 = 348^2 + 302^2 - 2x348x302x\cos 72$
		Total length = 1034m	A1	BC = 383.86
		(or better)	A1	Total length = BC + 650 ft
11	1a)	$-6 \le x \le 6$	A1	
	1b)	$-6 \le x \le 6$ $x \le -\frac{5}{3}, x \ge \frac{5}{3}$ $-\frac{10}{3} < x < 0$ $x < -\frac{1}{2} and x > \frac{3}{2}$	A1	
	1c)	$-\frac{10}{3} < x < 0$	A1	
	2	1 , 3	M1	Multiplying out denominators
		$x < -\frac{1}{2}$ and $x > \frac{1}{2}$	M1	Forming a single quadratic
			M1	2 critical values
				2 Citical values
			A1	
	3	4 > 2	M1	Factorising quadratic
		$x < -\frac{4}{3}, \qquad x > 2$	M1	Critical values
		_	A1	
12	1a)	(n+1) and (n+2)	A1	Both correct
	b)	= 3n + 3	M1	Adding expressions and simplifying result
		= 3 (n + 1)	M1	
		3 is a factor so the sum	A1	Factorising
		is a multiple of 3	'\1	Conclusion with reason
		is a multiple of 5		Conclusion with reason
	2	2n + 1 is an odd number	M1	Expression for odd number
				· ·
		$(2n + 1)^2 = 4n^2 + 4n + 1$	M1	Square expression
		$4n^2 + 4n = 4 (n^2 + 1) = even$	A1	Explanation
		so 4n ² + 4n + 1 is odd		



$ \begin{array}{c} 3 \\ = \frac{4x^{2}+5}{2(2x+5)} \\ = \frac{4x}{2} \\ = 2x \text{ which is always even as is} \\ = \frac{4x}{2} \\ = 2x \text{ which is always even as is} \\ = \frac{4x}{2} \\ = 2x \text{ which is always even as is} \\ = \frac{4x}{2} \\ = 2x \text{ which is always even as is} \\ = \frac{4x}{2} \\ = 2x \text{ which is always even as is} \\ = \frac{4x}{2} \\ = 2x \text{ which is always even as is} \\ = \frac{4x}{2} \\ = \frac{2x}{2} \\ = 2x \text{ which is always even as is} \\ = \frac{4x}{2} \\ = \frac{2x}{2} \\ =$	-				Partners in excellence
$=\frac{4x}{2}$ $=2x \text{ which is always even as is a multiple of 2}$ $=2x \text{ which is always even as is a multiple of 2}$ $=13$ $1(a)$ $=\frac{1}{3}(6h+2f+g) \text{ oe}$ $=1(b)$ $=\frac{1}{3}(6h+2f+g) \text{ oe}$ $=2$ $=3$ $=3$ $=3$ $=3$ $=3$ $=3$ $=3$ $=3$		3	$-\frac{4x(x^2+5)}{}$	M1	Factorise
2 x which is always even as is a multiple of 2			$-2(x^2+5)$		
2 x which is always even as is a multiple of 2			$-\frac{4x}{}$	M1	Simplify
13					
13			=2x which is always even as is	/ \ _	Explanation
			a multiple of 2		
	13	1(a)	-3h+2f+g	B1	OA - OB
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		· · ·			
BA = 3DC so lines are parallel M1 Expression for BA Expression for DC Concluding statement 3 QA and QM are both multiples of $2j - k$ so are parallel and have Q as a common point so are collinear 14 1 NP $\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$ M1 Multiplying each probability ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ PN $\frac{5}{12} \times \frac{3}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{1}{33}$ DD $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ Or (alternative solution)		1(6)	- - (6n + 21 + g) 6e		TO -TAIAO
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		1	DA 2DC so lines are negalial		Evangasian for DA
3 QA and QM are both multiples of $2j - k$ so are parallel and have Q as a common point so are collinear 14 1 NP $\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$ M1 Multiplying each probability ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ PN $\frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ PD $\frac{5}{12} \times \frac{4}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{5}{33}$ P(two different types) $= \frac{47}{66}$ Or (alternative solution) A1 Concluding statement M1 QA = 1/3 (2j - k) oe QM = 1/2 (2j - k) oe Concluding statement M1 M1 Multiplying each probability M1 Multiplying each probability M2 Adding their probabilities		2	BA = 3DC so lines are parallel		I
3 QA and QM are both multiples of $2\mathbf{j} - \mathbf{k}$ so are parallel and have Q as a common point so are collinear 14 1 1 1 1 1 1 1 1 1 1					
of $2\mathbf{j} - \mathbf{k}$ so are parallel and have Q as a common point so are collinear				A1	
14 1 NP $\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$ M1 Multiplying each probability ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ PN $\frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ PD $\frac{5}{12} \times \frac{4}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ Or (alternative solution)		3	QA and QM are both multiples	M1	
have Q as a common point so are collinear 14 1 NP $\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$ ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ PN $\frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ PD $\frac{5}{12} \times \frac{4}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{3}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ Or (alternative solution)			of 3i keep are norallel and	M1	· · · · · · · · · · · · · · · · · · ·
are collinear 14 1 NP $\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$ ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ PN $\frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ PD $\frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ Or (alternative solution)			or $2\mathbf{j} - \mathbf{k}$ so are parallel and	A1	Concluding statement
are collinear 14 1 NP $\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$ ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ PN $\frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ PD $\frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ Or (alternative solution)			have Q as a common point so		
14 1 NP $\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$ M1 Multiplying each probability ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ PN $\frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ PD $\frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ A1 Correct solution					
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$			are collinear		
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$ND \frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$ $PN \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$PN \qquad \frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$ $PD \qquad \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ $DN \qquad \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \qquad \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \qquad \text{Correct solution}$	14	1	$NP \qquad \frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$	M1	Multiplying each probability
PD $\frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ Or (alternative solution) A1 Correct solution			ND $\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$		
PD $\frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ DN $\frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ DP $\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ M1 Adding their probabilities P(two different types) = $\frac{47}{66}$ Or (alternative solution) A1 Correct solution			$PN = \frac{5}{2} \times \frac{3}{3} = \frac{5}{3}$		
$DN \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$ $DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $A1 \text{Correct solution}$					
$DP \frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$ $P(\text{two different types}) = \frac{47}{66}$ $Or (alternative solution)$ $M1 \text{Adding their probabilities}$ $A1 \text{Correct solution}$			$PD = \frac{5}{12} \times \frac{1}{11} = \frac{5}{33}$		
P(two different types) = $\frac{47}{66}$ Or (alternative solution) A1 Correct solution			$DN \qquad \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$		
P(two different types) = $\frac{47}{66}$ Or (alternative solution) A1 Correct solution			$DP = \frac{4}{10} \times \frac{5}{11} = \frac{5}{22}$	M1	Adding their probabilities
Or (alternative solution)			12 11 33		
			P(two different types) = $\frac{47}{66}$	A1	Correct solution
			Or (alternative solution)		
			NN $\frac{3}{12} \times \frac{2}{11} = \frac{1}{22}$	M1	Multiplying probability of same types

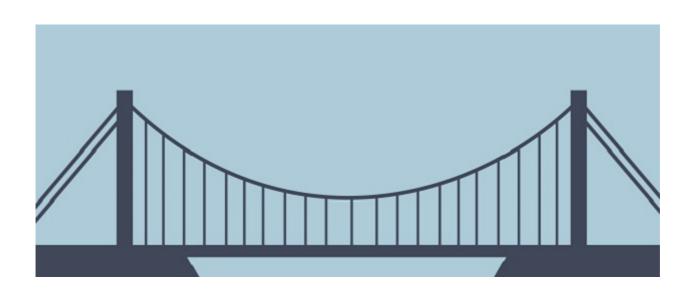


				Partners in excellence
		$PP \qquad \frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$		
		$DD \qquad \frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$		
		P(two the same type) = $1 - \frac{19}{66}$ = $\frac{47}{66}$	M1 A1	Subtracting their answer from 1 Correct solution
	2	$0.75 \times 0.7 = 0.525 \text{ or } 0.25 \times 0.9$	7.12	Multiplying probabilities for both
		= 0.225	M1	situations
		0.525 + 0.225	M1	Adding probabilities
		=0.75	A1	
	3a	13664 or 0.05	Λ 1	
	3a	13004 14345 or 0.95	A1	
	3b	$\frac{520}{12102} = \frac{260}{6051} \text{ or } 0.04$	A1	
	3c	$\frac{420}{13664} = \frac{15}{488} \text{ or } 0.03$	M1 A1	Allow M1 for $\frac{420}{14345} = \frac{84}{2869}$ or 0.03
15	1a	FD= 2.5 and 1.2	M1	FD = Frequency / class width
		Plot on graph	A1	
	1b	FD x class width	M1	Poth answers required
	2a	15 and 36 1.0, 3.7, 4.0, 1.5	A1 A1	Both answers required Frequency density calculated
	Za	1.0, 3.7, 7.0, 1.3	A1 A1	1 mark for 3 correct
		Correct histogram drawn	M1	Mark awarded for 2 correct bars All correct
			A1	
	2b	300 – 240 = 60 mins 90	M1 A1	Calculation to find the class width



The Bridge to A level

Diagnosis Worked Solutions





(2)

(4)

(3)

(1)

Solving quadratic equations 1

Question 1

Solve $x^2 + 6x + 8 = 0$

$$(x + 2)(x + 4) = 0$$

$$x = -2 \text{ or } -4$$

Question 2

Solve the equation $y^2 - 7y + 12 = 0$

Hence solve the equation $x^4 - 7x^2 + 12 = 0$

$$y^{2} - 7y + 12 = 0$$

$$(y - 3)(y + 4) = 0 \Rightarrow y = 3 \text{ or } y = 4$$

$$x^{4} - 7x^{2} + 12 = 0 \Rightarrow \text{ let } x^{2} = y$$

$$(x^{2})^{2} - 7x^{2} + 12 = 0 \Rightarrow y^{2} - 7y + 12 = 0 \Rightarrow y = 3 \text{ or } y = 4$$

$$\Rightarrow x^{2} = 3 \text{ or } x^{2} = 4$$

$$\Rightarrow x = \pm \sqrt{3} \text{ or } x = \pm 2$$

Question 3

Express $x^2 - 6x + 2$ in the form $(x-a)^2 - b$ (i)

$$x^{2}-6x+2 = (x-3)^{2}-9+2$$

$$= (x-3)^{2}-7$$

State the coordinates of the minimum value on the graph of $y = x^2 - 6x + 2$ (ii)



(3)

(3)

(4)

2 <u>Changing the subject</u>

Question 1

Make v the subject of the formula $E = \frac{1}{2} mv^2$

$$E = \frac{1}{2} m v^{2}$$

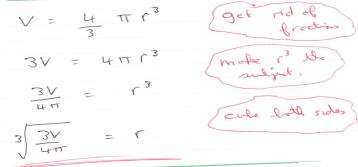
$$\Rightarrow 2E = m v^{2}$$

$$\Rightarrow \frac{2E}{m} = v^{2}$$

$$+ \sqrt{\frac{2E}{m}} = v$$

Question 2

Make r the subject of the formula $V = \frac{4}{3} \Pi r^2$



Question 3

Make c the subject of the formula $P = \frac{c}{c+4}$

$$P = C$$

$$C+4$$

$$P = C$$

$$C+4$$

$$Froting$$

$$P (C+4) = C$$

$$Expand lookets$$

$$P = C + HP = C$$

$$C = C + HP = C$$

$$C = C + HP = C$$

$$P = C + HP = C$$

$$C = C + P = C$$

$$C = C + P$$

$$C = C$$

$$C = C + P$$

$$C = C$$



(3)

(4)

3 <u>Simultaneous equations</u>

Question 1

Find the coordinates of the point of intersection of the lines y = 3x + 1 and x + 3y = 6

$$y = 3x + 1 \quad \text{and} \quad x + 3y = 6$$

$$x + 3(3x + 1) = 6$$

$$x + 9x + 3 = 6$$

$$10x = 3$$

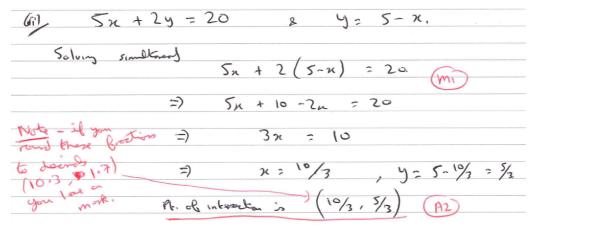
$$x = \frac{3}{10}$$

$$x = \frac{9}{10} + 1$$

$$= \frac{9}{$$

Question 2

Find the coordinates of the point of intersection of the lines 5x + 2y = 20 and y = 5 - x



Question 3

Solve the simultaneous equations

$$x^2 + y^2 = 5$$
 $y = 3x + 1$

Sub is
$$y = 3x + 1$$
 is expressed 2.
 $x^{2} + (3x + 1)^{2} = 5$
 $x^{2} + (3x + 1)(3x + 1) = 5$
 $y = (3x^{\frac{2}{5}}) + 1$
 $x^{2} + 9x^{2} + 3x + 3x + 1 = 5$
 $10x^{2} + 6x + 1 = 5$
 $10x^{2} + 6x - 4 = 0$
 (-2)
 $5x^{2} + 3x - 2 = 0$
 $(5x - 2)(x + 1) = 0$
 $x = -2$
 $(5x - 2)(x + 1) = 0$
 $x = -2$



(2)

(2)

(3)

4 Surds

Question 1

(i) Simplify $(3 + \sqrt{2})(3 - \sqrt{2})$

$$(3+52)(3-52)$$
= $3^2 + 352 - 352 - (52)^2$
= 7

(ii) Express $\frac{1+\sqrt{2}}{3-\sqrt{2}}$ in the form $a+b\sqrt{2}$ where a and b are rational

$$\frac{(1+\sqrt{52})}{(3-\sqrt{52})} = \frac{(1+\sqrt{52})(3+\sqrt{52})}{(3-\sqrt{52})(3+\sqrt{52})}$$

$$= \frac{3+\sqrt{52}+3\sqrt{52}+(\sqrt{52})^2}{7}$$

$$= \frac{3+\sqrt{52}+3\sqrt{52}+(\sqrt{52})^2}{7}$$

$$= \frac{3+\sqrt{52}+3\sqrt{52}+(\sqrt{52})^2}{7}$$

$$= \frac{3+\sqrt{52}+3\sqrt{52}+(\sqrt{52})^2}{7}$$

$$= \frac{3+\sqrt{52}+3\sqrt{52}+(\sqrt{52})^2}{7}$$

$$= \frac{3+\sqrt{52}+3\sqrt{52}}{7}$$

Question 2

(i) Simplify $5\sqrt{8} + 4\sqrt{50}$. Express your answer in the form $a\sqrt{b}$ where a and b are integers and b is as small as possible.

(ii) Express $\frac{\sqrt{3}}{6-\sqrt{3}}$ in the form $p+q\sqrt{3}$ where p and q are rational

$$\frac{\sqrt{3}}{6-\sqrt{3}} = \frac{\sqrt{3}}{6-\sqrt{3}} \times \frac{(6+\sqrt{3})}{(6+\sqrt{3})}$$

$$= \frac{\sqrt{3} \times 6 + \sqrt{3}\sqrt{3}}{6^2 - (\sqrt{3})^2}$$

$$= \frac{\sqrt{3} \times 6 + \sqrt{3}\sqrt{3}}{36-3}$$

$$= \frac{3}{33} + \frac{6}{33}$$

$$= \frac{3}{33} + \frac{6}{33}$$

$$= \frac{1}{11} + \frac{2}{11}\sqrt{3}.$$

Total / 10

5



5 <u>Indices</u>

Question 1

Simplify the following

(i) a^c

(ii)
$$a^6 \div a^{-2}$$

(iii) $(9a^6b^2)^{-0.5}$

(i)
$$a^{\circ} = 1$$

(ii) $a^{\circ} = 1$
 $= a^{\circ} = 1$

Question 2

(i) Find the value of $\left(\frac{1}{25}\right)^{-0.5}$

(ii) Simplify $\frac{(2x^2y^3z)^5}{4y^2z}$

(3)
$$\frac{1}{25} = (25)^{\frac{1}{2}} = \sqrt{25} = \pm 5$$

$$\frac{2x^{2}y^{3}z}{4y^{2}z} = \frac{25}{2y^{2}z^{1}}$$

$$= 2x^{2}y^{3}z^{2} = 2x^{2}y^{3}z^{4}$$

$$= 2x^{2}y^{3}z^{4} = 8x^{2}y^{3}z^{4}$$



(3)

6 <u>Properties of Lines</u>

Question 1

A (0,2), B (7,9) and C (6,10) are three points.

(i) Show that AB and BC are perpendicular

Grad of AB =
$$\frac{9-2}{7-0}$$
 = 1

Grad of BC =
$$\frac{10-9}{6-7}$$
 = -1

Product of gradients = $1 \times -1 = -1 \rightarrow AB$ and BC perpendicular

(ii) Find the length of AC

$$(6-0)^2 + (10-2)^2 = AC^2$$

AC = 10

Question 2 (2)

Find, in the form y = mx + c, the equation of the line passing through A (3,7) and B (5,-1). Show that the midpoint of AB lies on the line x + 2y = 10

$$m = \frac{-1-7}{5-3} = \frac{-8}{2} = -4$$

$$y = -4x + C$$
Substitute in (3,7) [5,1] would do equally as well
$$7 = -4x3 + C$$

$$19 = C$$

$$y = -4x + 19$$

Midpoil of AB =
$$(24,3)$$

Sub. in to $x+2y=10$ 8 show
Abd exporting is true.
 $24+2\times3=4+6=10$
TRUE.

(5)



(3)

(3)

7 **Sketching curves**

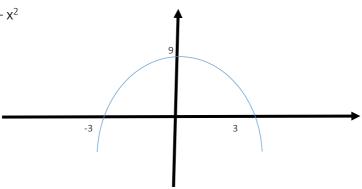
Question 1

In the cubic polynomial f(x), the coefficient of x^3 is 1. The roots of f(x) = 0 are -1, 2 and 5. Sketch the graph of y = f(x)



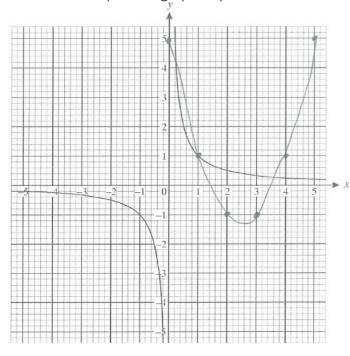
Question 2

Sketch the graph of $y = 9 - x^2$



Question 3

The graph below shows the graph of $y = \frac{1}{x}$ On the same axes plot the graph of $y = x^2 - 5x + 5$ for $0 \le x \le 5$



70	0	1	2	3	4	5
X	0	1	4	9	16	25
-5x	0	-5	-10	-15	-20	-25
+5	+5	+5	+5	+5	+5	+5
<u>J</u>	5		-1		1	5

(4)



8 <u>Transformation of functions</u>

Question 1

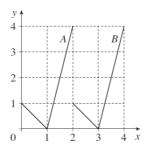
The curve $y = x^2 - 4$ is translated by $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$

Write down an equation for the translated curve. You need not simplify your answer.

$$y = (x-2)^2 - L_f \tag{2}$$

Question 2

This diagram shows graphs A and B.



(i) State the transformation which maps graph A onto graph B



(ii) The equation of graph A is y = f(x).

Which one of the following is the equation of graph B?

$$y = f(x) + 2$$

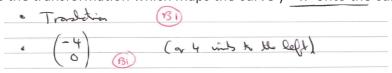
$$y = f(x) - 2$$

$$y = f(x+2)$$

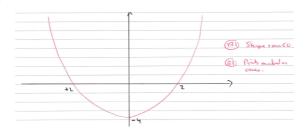
$$y = f(x-2)$$

Question 3

(i) Describe the transformation which maps the curve $y = x^2$ onto the curve $y = (x+4)^2$



(ii) Sketch the graph of $y = x^2 - 4$



(2)

(2)

(2)

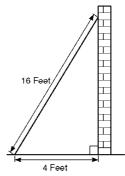
(2)



9 Trigonometric ratios

Question 1

Sidney places the foot of his ladder on horizontal ground and the top against a vertical wall. The ladder is 16 feet long.



The foot of the ladder is 4 feet from the base of the wall.

(i) Work out how high up the wall the ladder reaches. Give your answer to 3 significant figures.

 $\sqrt{16^2 - 4^2}$

√256 -16 correct substitution (M1)

√240

15.49

(ii) Work out the angle the base of the ladder makes with the ground. Give your answer to 3 sig fig $\cos x = \frac{4}{16}$ correct ratio and substitution (M1)

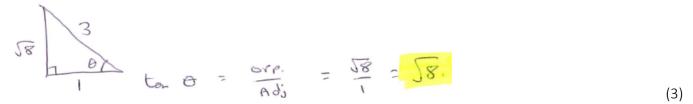
 $\cos x = 0.25$

x = 75.522

$$x = 75.5^{\circ}$$
 (A1)

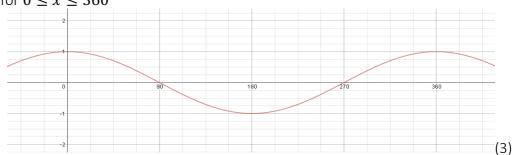
Question 2

Given that $\cos \Theta = \frac{1}{3}$ and Θ is acute, find the exact value of $\tan \Theta$



Question 3

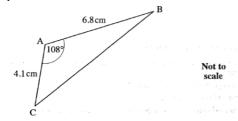
Sketch the graph of $y = \cos x$ for $0 \le x \le 360^{\circ}$





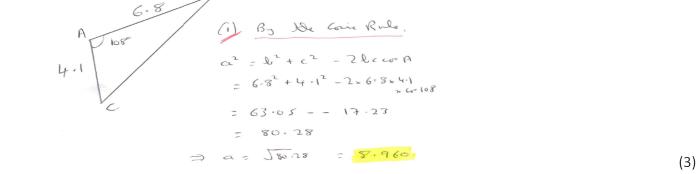
10 Sine / Cosine Rule

Question 1



For triangle ABC, calculate

(i) the length of BC

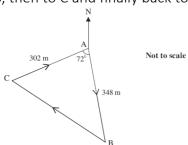


(ii) the area of triangle ABC



Question 2

The course for a yacht race is a triangle as shown in the diagram below. The yachts start at A, then travel to B, then to C and finally back to A.



Calculate the total length of the course for this race.

$$C = \frac{302}{72^{\circ}}$$

$$C = \frac{302^{\circ} + 348^{\circ}}{348}$$

$$C = \frac{302^{\circ} + 348^{\circ}}{384^{\circ}} - 2 \times 302 \times 348 \times 672$$

$$C = \frac{384}{384^{\circ}}$$

$$Total length = 384 + 650 = 1034m$$
(4)



11 <u>Inequalities</u>

Question 1

Solve

a)
$$x^2 - 36 \le 0$$

$$(x+6)(x-6) \le 0$$

-6 \le x \le 6 (A1)

b)
$$9x^2 - 25 \ge 0$$

$$(3x-5)(3x+5) \ge 0$$

 $x \le -\frac{5}{3}, x \ge \frac{5}{3}$ (A1)

c)
$$3x^2 + 10x < 0$$

$$x(3x+10) < 0$$

$$-\frac{10}{3} < x < 0$$
 (A1)

(3)

Question 2

Solve

$$\frac{21}{x+2} - \frac{5}{x+1} < 4$$

$$21(x+1) - 5(x+2) < 4(x+2)(x+1)$$
 (M1)

$$21x + 21 - 5x - 10 < 4(x^2 + 3x + 2)$$

$$16x + 11 < 4x^2 + 12x + 8$$

$$0 < 4x^2 - 4x - 3 \tag{M1}$$

$$0 < (2x+1)(2x-3)$$

Critical values
$$x = -\frac{1}{2} or x = \frac{3}{2}$$
 (M1)

$$x < -\frac{1}{2} and x > \frac{3}{2} \tag{A1}$$

....(4)

Question 3

Solve $3x^2 - 8 > 2x$

$$3x^2 - 2x - 8 > 0$$

(3x + 4)(x - 2) > 0 (M1)

Critical values
$$x = -4/3$$
 and $x=2$ (M1)

$$x < -\frac{4}{3}$$
, $x > 2$ (A1)

(3)



12 <u>Algebraic proof</u>

Question 1

a) If n is a positive integer, write down expressions for the next two consecutive integers.

$$(n+1)$$
 and $(n+2)$

1M both correct

(1)

b) Use algebra to prove that the sum of three positive consecutive integers is always a multiple of 3.

$$n + n + 1 + n + 2$$

$$= 3n + 3$$

$$= 3 (n + 1)$$

3 is a factor so the sum is a multiple of 3

- Adding expressions and simplifying result
- Factorising
- Conclusion with reason

(3)

Question 2

Prove that the square of an odd number is also odd.

2n is an even number then 2n + 1 is an odd number

$$(2n + 1)^2 = 4n^2 + 4n + 1$$

 $4n^2 + 4n = 4$ ($n^2 + 1$) so this expression is a multiple of 4 hence even so $4n^2 + 4n + 1$ is odd

- Writing algebraic expression for odd number
- Squaring expression
- Explain why result is odd

(3)

Question 3

Given that x is a positive integer, prove that $\frac{4x^3+20x}{2x^2+10}$ is always even

$$=\frac{4x(x^2+5)}{2(x^2+5)}$$

$$=\frac{4x}{2}$$

$$=\frac{}{2}$$

= 2x which is always even as is a multiple of 2

- Factorise
- Simplify
- Explain why result is even

(3)



13 **Vectors**

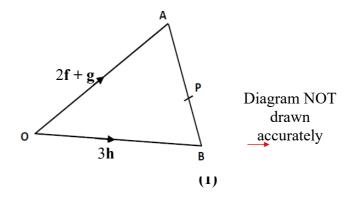
Question 1

OAP is a triangle

$$OA = 2\mathbf{f} + \mathbf{g}$$
 and $OB = 3\mathbf{h}$

P is the point on AB such that AP: PB = 2:1

(a) Find the vector \overrightarrow{BA} in terms of \mathbf{f} , \mathbf{g} and \mathbf{h} .



(b) Find the vector \overrightarrow{PO} in terms of \mathbf{f} , \mathbf{g} and \mathbf{h}

$$\overrightarrow{PO} = \overrightarrow{PA} + \overrightarrow{AO} = \frac{2}{3}(-3\mathbf{h} + 2\mathbf{f} + \mathbf{g}) - (2\mathbf{f} + \mathbf{g}) \text{ (M1)}$$

$$\overrightarrow{PO} = -2\mathbf{h} - \frac{2}{3}\mathbf{f} - \frac{1}{3}\mathbf{g} \text{ or } -\frac{1}{3}(6\mathbf{h} + 2\mathbf{f} + \mathbf{g}) \text{ oe simplified expression (A1)}$$

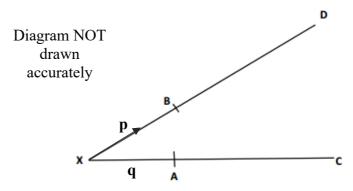
(2)

Question 2

B is the point on AD such that XB:BD is

A is the point on XC such that XA:XC is 1:2

$$XB = \mathbf{p}$$
 and $XA = \mathbf{q}$



Use vectors to explain the geometrical relationships between the line segments BA and DC.

$$\overrightarrow{BA} = -p + q (M1)$$

$$\overrightarrow{DC} = -3p + 3q (M1)$$

 $\overrightarrow{BA} = \overrightarrow{3DC}$ so the lines are parallel (A1) and DC is 3 times the length of BA (A1)

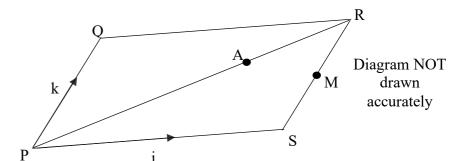


Question 3

PQRS is a parallelogram.

A is the point on PR such that PA:AR is 2:1

M is the midpoint of RS.



(b) Prove that Q, A and M are co-linear.

$$\overrightarrow{QA} = -\mathbf{k} + 2/3(\mathbf{k} + \mathbf{j}) = -1/3\mathbf{k} + 2/3\mathbf{j} = 1/3 (2\mathbf{j} - \mathbf{k})$$
 (M1) accept any equivalent vector
$$\overrightarrow{QM} = -\mathbf{k} + \mathbf{j} + \frac{1}{2} \mathbf{k} = -1/2 \mathbf{k} + \mathbf{j} = \frac{1}{2} (2\mathbf{j} - \mathbf{k})$$
 (M1) accept any equivalent vector

 \overrightarrow{QA} and \overrightarrow{QM} are both multiples of $2\mathbf{j} - \mathbf{k}$ so are parallel and have Q as a common point so are collinear

(3)



14 <u>Probability</u>

Question 1

A box contains 3 new batteries, 5 partly used batteries and 4 dead batteries.

Kelly takes two batteries at random.

Work out the probability that she picks two different types of batteries.

NP	$\frac{3}{12} \times \frac{5}{11} = \frac{5}{44}$		
ND	$\frac{3}{12} \times \frac{4}{11} = \frac{1}{11}$		
PN	$\frac{5}{12} \times \frac{3}{11} = \frac{5}{44}$		
PD	$\frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$	Multiplying each probability	M1
DN	$\frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$	Adding their probabilities	M1
DP	$\frac{4}{12} \times \frac{5}{11} = \frac{5}{33}$	Correct solution	A1

P(two different types) = $\frac{47}{66}$

Or

NN $\frac{3}{12} \times \frac{2}{11} = \frac{1}{22}$ PP $\frac{5}{12} \times \frac{4}{11} = \frac{5}{33}$ DD $\frac{4}{12} \times \frac{3}{11} = \frac{1}{11}$

Multiplying probability of MTS by 6 M1

Subtracting their answer from 1 M1
Correct solution A1

P(two the same type) = $1 - \frac{19}{66} = \frac{47}{66}$

(3)

Question 2

Caleb either walks to school or travels by bus.

The probability that he walks to school is 0.75.

If he walks to school, the probability that he will be late is 0.3.

If he travels to school by bus, the probability that he will be late is 0.1.

Work out the probability that he will not be late.

$$0.75 \times 0.7 = 0.525$$
 or $0.25 \times 0.9 = 0.225$ M1 $0.525 + 0.225 =$ M1 0.75

(3)



Question 3

he two way table shows the number of deaths and serious injuries caused by road traffic accidents in Great Britain in 2013.

		Speed Limit			
		20 mph	30 mph	40 mph	Total
	Fatal	6	520	155	681
Type of Injury	Serious	420	11582	1662	13664
	Total	426	12102	1817	14345

(a) that the accident is serious.

13664	or	0.95
14345	OI	0.53

Α1

(1)

(b) that the accident is fatal given that the speed limit is 30 mph.

$$\frac{520}{12102} = \frac{260}{6051} \text{ or } 0.04$$

(c) that the accident happens at 20 mph given that the accident is serious.

$$\frac{420}{13664} = \frac{15}{488}$$
 or 0.03

M2 (Correct working must be seen)

Allow M1 for
$$\frac{420}{14345} = \frac{84}{2869}$$
 or 0.03

(2)

(1)



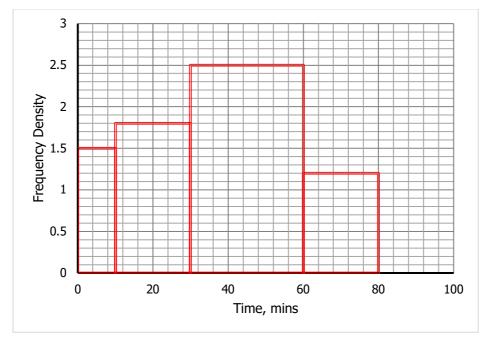
15 <u>Statistics</u>

Question 1

The histogram and the frequency table show some information about how much time vehicles spent in a car park.

Time, minutes			Frequency
0	< X ≤	10	15
10	< x ≤	30	36
30	< x ≤	60	75
60	< x ≤	80	24
		Total	150

Class Width	Freq. Density
10	1.5
20	1.8
30	2.5
20	1.2



a) Use the information to complete the histogram

b) Use the histogram to find the missing frequencies in the table

......15 and 36

(2)

(2)

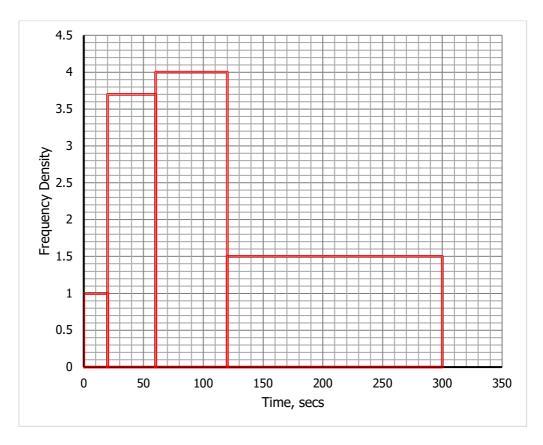


Question 2

The table shows the length of 678 phone calls made at a call centre

Time, secs		Frequency	Class Width	Freq. Density	
0	< x ≤	20	20	20	1.0
20	< x ≤	60	148	40	3.7
60	< x ≤	120	240	60	4.0
120	< x ≤	300	270	180	1.5
		Total	678		

a) Draw a fully labelled histogram to show the length of the phone calls.



b) Estimate the number of phone calls that lasted more than 4 minutes.

4 minutes = 4 x 60 secs = 240 secs 300 - 240 = 60 mins 60 x 1.5 = (90 calls) M1

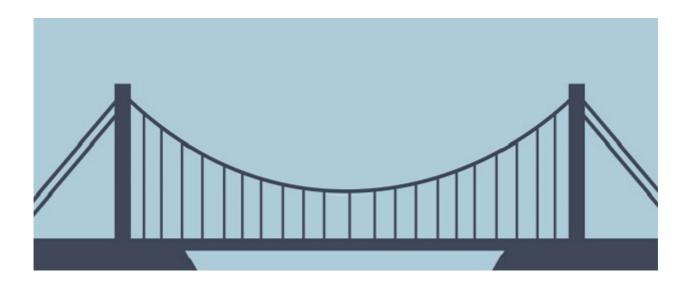
.....90 calls.....A1....(2)

(4)



The Bridge to A level

Therapy





Therapy for Topics

All therapy references are referenced to the *PiXL Maths App* or *MyMaths*

For the *PiXL Maths App* you need to navigate to the *Therapy* videos as follows:

After logging in, select the *Design a Test* tab.

This will give you 7 tabs to choose from (Number, Algebra, Ratio & Proportion, Geometry, Probability, Statistics and Problem Solving). Select one of these; this is the *Topic*.

You will now see a menu of *Test Titles*. Select the one you need, and you will need to select the *Begin Test* button.

You need not do this test, but it will bring up the *Therapy Video* button which you now select.

This will give you the menu of Therapy video titles applicable to this test, Select the one you need.

<u>In Summary</u>, all therapy references are for therapy videos from the PiXL Maths App. The relevant video is found by accessing

Design a Test / Topic / Test Title / Therapy video title

The PiXL Maths App can be downloaded free from the PiXL website

http://mathsapp.pixl.org.uk/

For *MyMaths* your school needs to supply you with your login details.

The hyperlinks in this document will take you directly to the pages you will need. (You may need to copy and paste the link into your web browser).



Therapy for Topic 1

Quadratic equations

PiXL Therapy - Rearranging and solving quadratics, Completing the square, Factorising, Formula

Maths App Reference

- 1. Algebra / Graph transformations part a / Calculate the minimum point of a quadratic function
- 2. Algebra / Quadratics / Solve a quadratic by factorising where a is not 1 **and** solve a quadratic by completing the square

MyMaths Reference

https://app.mymaths.co.uk/1784-resource/quadratic-equations-1

https://app.mymaths.co.uk/192-resource/quadratic-equations-2

https://app.mymaths.co.uk/193-resource/completing-the-square

https://app.mymaths.co.uk/194-resource/quadratic-formula

Therapy for Topic 2

Algebra

Maths App Reference

1. Algebra / Harder equations and re-arranging formulae / Re-arrange a formula where the subject appears more than once

MyMaths Reference

https://app.mymaths.co.uk/175-resource/factorising-quadratics-2

https://app.mymaths.co.uk/207-resource/rearranging-2

https://app.mymaths.co.uk/176-resource/cancelling-algebraic-fractions

https://app.mymaths.co.uk/177-resource/adding-algebraic-fractions

https://app.mymaths.co.uk/178-resource/multiplying-algebraic-fractions

Therapy for Topic 3

Simultaneous equations

PiXL Therapy - Linear, Non-linear

Maths App Reference

1. Algebra / Simultaneous equations / Solve linear and non-linear simultaneous equations

MyMaths Reference

https://app.mymaths.co.uk/198-resource/simultaneous-equations-3 https://app.mymaths.co.uk/195-resource/quadratic-simultaneous-equa

Therapy for Topic 4

Surds

PiXL Therapy - Surds

Maths App Reference

- 1. Number / Surds / Simplify a surd
- 2. Number / Surds / Rationalise a denominator



3. Number / Surds / Operate with surds

MyMaths Reference

https://app.mymaths.co.uk/599-resource/surds-part-1 https://app.mymaths.co.uk/600-resource/surds-part-2

Therapy for Topic 5

Indices

PiXL Therapy - Negative and fractional index laws

Maths App Reference

1. Number / Indices / Evaluate positive, negative and fractional indices

MyMaths Reference

https://app.mymaths.co.uk/597-resource/indices-part-2 https://app.mymaths.co.uk/598-resource/indices-part-3

Therapy for Topic 6

Properties of lines

MyMaths Reference

https://app.mymaths.co.uk/559-resource/equation-of-a-line https://app.mymaths.co.uk/3270-resource/equation-of-a-line-3

Therapy for Topic 7

Sketching curves

PiXL Therapy - Turning points and completing the square

MyMaths Reference

https://app.mymaths.co.uk/226-resource/sketching-quadratic-graphs-2 https://app.mymaths.co.uk/3266-resource/sketching-cubic-graphs https://app.mymaths.co.uk/588-resource/sketching-polynomials

Therapy for Topic 8

Transformation of functions

PiXL Therapy - <u>Translate a function</u>

Maths App Reference

- 1. Algebra/ Graph transformations part a / Recognise the shape of quadratic graph transformations
- 2. Algebra / Graph transformations part a / Calculate the minimum point of a quadratic function
- 3. Algebra / Graph transformations part b / Recognise trigonometric graph transformations
- 4. Algebra / Graph transformations part b / Interpret values from a transformed trigonometric graph

MyMaths Reference

https://app.mymaths.co.uk/585-resource/transforming-graphs



https://app.mymaths.co.uk/3265-resource/transforming-graphs-1 https://app.mymaths.co.uk/229-resource/transforming-graphs-2

Therapy for Topic 9 Pythagoras' Theorem and Trigonometric ratios

Maths App Reference

- 1. Geometry / Trigonometry / Calculate an unknown angle or side using SOH CAH TOA
- 2. Geometry / Trigonometry / Apply Pythagoras' Theorem and SOH CAH TOA in 3D contexts
- 3. Geometry / Pythagoras' Theorem / Calculate the length of a line in 2D or 3D problems and Calculate the length of a line using Pythagoras from coordinates

MyMaths Reference

https://app.mymaths.co.uk/300-resource/pythagoras-theorem

https://app.mymaths.co.uk/301-resource/pythagoras-3d

https://app.mymaths.co.uk/321-resource/trig-missing-angles

https://app.mymaths.co.uk/322-resource/trig-missing-sides

https://app.mymaths.co.uk/328-resource/3d-trigonometry

Therapy for Topic 10

Sine / Cosine Rule

PiXL Therapy - Cosine rule, Sine rule

Maths App Reference

- 1. Geometry / Sine and Cosine Rules / Apply the sine and cosine rules to calculate a length or an angle
- 2. Geometry / Sine and Cosine Rules / Calculate the area of non-right angled triangles and of a segment.

MyMaths Reference

https://app.mymaths.co.uk/325-resource/cosine-rule-sides

https://app.mymaths.co.uk/326-resource/cosine-rule-angles

https://app.mymaths.co.uk/324-resource/sine-rule

https://app.mymaths.co.uk/327-resource/trig-area-of-a-triangle

Therapy for Topic 11 Inequalities

PiXL Therapy - Quadratic inequalities

Maths App Reference

1. Algebra / Inequalities / Solve inequalities

MyMaths Reference

https://app.mymaths.co.uk/232-resource/inequations

https://app.mymaths.co.uk/235-resource/quadratic-inequalities

Therapy for Topic 12 Algebraic Proof



PiXL Therapy - Proof

MyMaths Reference

https://app.mymaths.co.uk/1781-resource/identities https://app.mymaths.co.uk/1777-resource/proof

Therapy for Topic 13 Vectors

PiXL Therapy - Vectors

Maths App Reference

- 1. Geometry / Vectors / Construct a resultant vector from a diagram
- 2. Geometry / Vectors / Recognise when 3 or more points are collinear
- 3. Geometry / Vectors / Perform vector arithmetic

MyMaths Reference

https://app.mymaths.co.uk/332-resource/vectors-1 https://app.mymaths.co.uk/333-resource/vectors-2

Therapy for Topic 14 Probability

PiXL Therapy - Conditional probability

Maths App Reference

- 1. Probability / Dependent events / Calculate probabilities from tree diagrams using AND / OR statements
- 2. Probability / Venn diagrams part b / Calculate probability from Venn diagrams and set notation

MyMaths Reference

https://app.mymaths.co.uk/1730-resource/venn-diagrams-2

https://app.mymaths.co.uk/381-resource/probability-revision

https://app.mymaths.co.uk/382-resource/the-or-rule

https://app.mymaths.co.uk/383-resource/independent-probability

Therapy for Topic 15 Statistics: Averages and Graphs

PiXL Therapy - <u>Histograms</u>

Maths App Reference

- 1. Statistics / Histogram tables / Calculating the frequency density
- 2. Statistics / Interpreting histograms / Calculating the frequency from a histogram



- 3. Statistics / Averages from a frequency table / Calculate the mean from a grouped frequency table
- 4. Statistics / Frequency polygon graphs / Interpret values from a frequency polygon graph
- 5. Statistics / Cumulative frequency graphs / Interpret a cumulative frequency diagram
- 6. Statistics / Boxplots / Interpret a boxplot

MyMaths Reference

https://app.mymaths.co.uk/365-resource/histograms

https://app.mymaths.co.uk/1739-resource/frequency-polygons

https://app.mymaths.co.uk/362-resource/cumulative-frequency-1

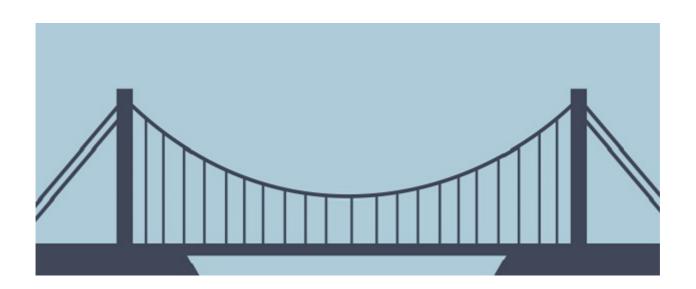
https://app.mymaths.co.uk/363-resource/cumulative-frequency-2

https://app.mymaths.co.uk/364-resource/box-and-whisker-plots



The Bridge to A level

Test yourself





1 Solving quadratic equations

Question 1

Find the real roots of the equation $x^4 - 5x^2 - 36 = 0$ by considering it as a quadratic equation in x^2

(4)

Question 2

(i) Write $4x^2 - 24x + 27$ in the form of $a(x - b)^2 + c$

(4)

(ii) State the coordinates of the minimum point on the curve $y = 4x^2 - 24x + 27$.

(2)



2 <u>Changing the Subject</u>

Question 1

Make t the subject of the formula $s = \frac{1}{2}at^2$

(3)

Question 2

Make x the subject of 3x - 5y = y - mx

(3)

Question 3

Make x the subject of the equation $y = \frac{x+3}{x-2}$

(4)



3 Simultaneous equations

Question 1

Find the coordinates of the point of intersection of the lines x + 2y = 5 and y = 5x - 1

(3)

Question 2

The lines y = 5x - a and y = 2x + 18 meet at the point (7,b).

Find the values of *a* and *b*.

(3)

Question 3

A line and a curve has the following equations:

$$3x + 2y = 7$$

$$y = x^2 - 2x + 3$$

Find the coordinates of the points of intersection of the line and the curve by solving these simultaneous equations algebraically

(4)



4 <u>Surds</u>

Question 1

(i) Simplify $\sqrt{24} + \sqrt{6}$

(ii) Express $\frac{36}{5-\sqrt{7}}$ in the form $a+b\sqrt{7}$, where a and b are integers.

(3)

(2)

(2)

Question 2

(i) Simplify $6\sqrt{2} \times 5\sqrt{3} - \sqrt{24}$

(ii) Express (2 - $3\sqrt{5}$)² in the form $a + b\sqrt{5}$, where a and b are integers.

(3)

(2)

(2)

(2)

5 <u>Indices</u>

Question 1

Find the value of the following.

- (i) $\left(\frac{1}{3}\right)^{-2}$
- (ii) $16^{\frac{3}{4}}$

Question 2

- (i) Find a, given that $a^3 = 64x^{12}y^3$
- (ii) $\left(\frac{1}{2}\right)^{-5}$

Question 3
Simplify $\frac{16^{\frac{1}{2}}}{3}$

(2)



6	<u>Properties of Lines</u>	
Quest	tion 1	
The po	oints A (-1,6), B (1,0) and C (13,4) are joined by straight lines. Prove that AB and BC are perpendicul	lar.
		(2)
Quest	tion 2	
A and AB.	B are points with coordinates (-1,4) and (7,8) respectively. Find the coordinates of the midpoint, N	1, of
		(1)
Quest	tion 3	
	has gradient -4 and passes through the point (2,-6). Find the coordinates of its points of intersection has axes.	n
		(4)
0		(4)
Quest	tion 4	
	he equation of the line which is parallel to $y = 3x + 1$ and which passes through the point with linates (4,5).	
		(3)

7 <u>Sketching curves</u>

Question 1

You are given that f(x) = (x + 1)(x - 2)(x - 4)

Sketch the graph of y = f(x)

(3)

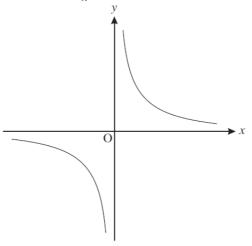
Question 2

Sketch the graph of $y = x(x - 3)^2$

(3)

Question 3

This diagram shows a sketch of the graph of $y = \frac{1}{x}$



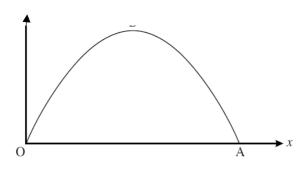
Sketch the graph of $y = \frac{1}{x-2}$, showing clearly any points where it crosses the axes.

(3)



Question 4

This curve has equation $y = \frac{1}{5}x (10 - x)$. State the value of x at the point A.



Total / 10

(1)



8 <u>Transformation of functions</u>

Question 1

The graph of $y = x^2 - 8x + 25$ is translated by $\begin{pmatrix} 0 \\ -20 \end{pmatrix}$.

State an equation for the resultant graph.

(1)

Question 2

$$f(x) = x^3 - 5x + 2$$

Show that $f(x-3) = x^3 - 9x^2 + 22x - 10$

(4)

Question 3

You are given that $f(x) = 2x^3 + 7x^2 - 7x - 12$

Show that $f(x-4) = 2x^3 - 17x^2 + 33x$

(3)

Question 4

You are given that f(x) = (x + 1)(x - 2)(x - 4).

The graph of y = f(x) is translated by $\binom{3}{0}$.

State an equation for the resulting graph. You need not simplify your answer.

(2)



9 <u>Trigonometric ratios</u>

Question 1

AP is a telephone pole. The angle of elevation of the top of the pole from the point R on the ground is 42°as seen in the diagram.



Calculate the height of the pole. Give your answer to 3 significant figures.

(3)

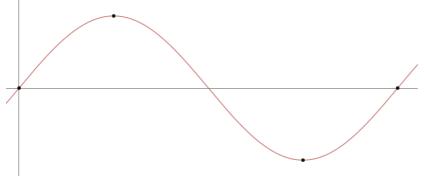
Question 2

Given that $\sin \Theta = \frac{\sqrt{3}}{4}$, find in surd form the possible values of $\cos \Theta$.

(3)

Question 3

The graph of $y = \sin x$ for $0 \le x \le 360^{\circ}$ is shown below.



What are the coordinates of the 4 points labelled on the graph?

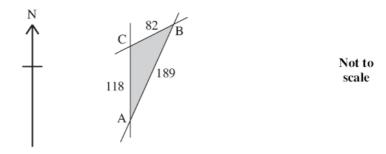
,)
,)
,)
,)
	(4)



10 Sine / Cosine Rule

Question 1

This diagram shows a village green which is bordered by 3 straight roads AB, BC and AC. The road AC runs due North and the measurements are shown in metres.



- (i) Calculate the bearing of B from C, giving your answer to the nearest 0.1°
- (ii) Calculate the area of the village green.

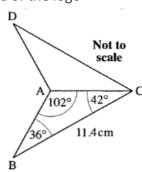
(2)

(4)

Question 2

This diagram shows a logo ABCD. It is symmetrical about AC.

Find the length of AB and hence find the area of the logo



(4)



11 <u>Inequalities</u>

Question 1

Solve the inequality $x^2 < 3(x+6)$

(3)

Question 2

Solve the inequality $x^2 > 3x + 4$

(3)

Question 3

A rectangle has length 3x cm and width (x+2) cm. The area of the rectangle is less than 90cm. Find the possible range of values for x.

(4)



12 <u>Algebraic proof</u>

Question 1

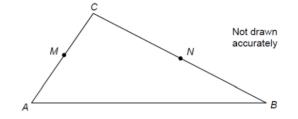
Quest	ion 1	
a)	If n is a positive integer explain why the expression 2n + 1 is always an odd number.	
b)	Use algebra to prove that the product of two odd numbers is also odd.	(1)
		(4)
Quest	ion 2	
a)	Prove that the sum of four consecutive whole numbers is always even.	
		(3)
b)	Give an example to show that the sum of four consecutive number is not always divisible by 4.	
		(2)
	Total / 10	



13 <u>Vectors</u>

Question 1

Triangle ABC has points M as the midpoints of AC and point N such that BN:CN = 2:3



$$\overrightarrow{AM} = a$$
$$\overrightarrow{AB} = 2b$$

a) Calculate \overrightarrow{MN} giving your answer in its simplest form.

b) Are the lines MN and AB parallel? Show all of your working.

(4)

(1)

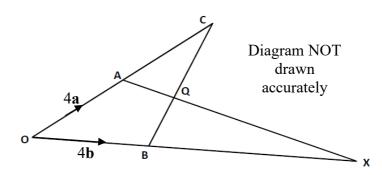
Question 2

In the diagram

OA = 4**a** and OB = 4**b** A is the midpoint of OC

BQ:QC = 1:2

Find, in terms of ${\bf a}$ and ${\bf b}$, the vector that represents



(a) BC

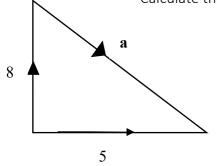
(b) AQ

(2)



Question 3

Calculate the magnitude of vector **a.**



(2)



14 <u>Probability</u>

Question 1

Laura has 9 tins of soup in her cupboard, but all the labels are missing.

She knows that there are 5 tins of tomato soup and 4 tins of vegetable soup.

She opens three tins at random.

Work out the probability that she opens more tins of vegetable soup than tomato soup.

		(4)
Question 2		
A summer camp runs coasteering and surfing classes.		
50 children attend the camp 35 children do coasteering 10 children do both classes 2 children do neither class a) Draw a venn diagram to represent this information		
8		
A child attending the summer camp is selected at random.		(2)
b) Find the probability that the child		
i) did exactly one class		
		(2)
ii) did surfing, given that they did not do coasteering		
		(2)
	Total / 10	



15 <u>Statistics</u>

Question 1

The table and histogram show the lengths of some pythons.

Le	ength, c	Frequency	
30	< x ≤	40	20
40	< x <	50	10
50	< x <	70	50
70	< x ≤	100	
100	< x ≤	150	
	•	Total	

2.5 2.5 1.5 0.5 0 50 100 150 200 Length, cms

/ \		1				
(a)	Use the	histogram	to find t	he missing	trequencies	s in the table

(2)

(b) Estimate the median python length.

....(3)

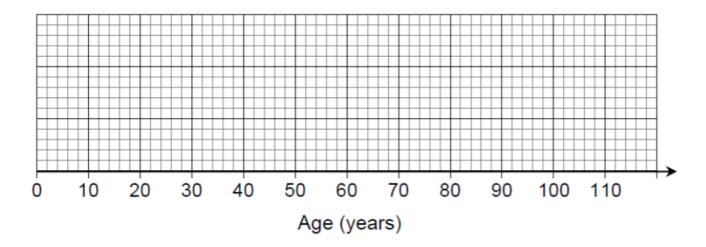
(Total 5 marks)



Question 2

In France in 2007 25% of the population were under 21years old. 50% were under 36. The interquartile range of the ages was 30 years. The oldest person was 103 years old.

a) Show this information on a boxplot



b) It is predicted that by 2040 the age distribution in France will have a lower quartile of 26 years, a median of 44 years and an upper quartile of 66 years.

Make two comments about the predicted change in the age distribution from 2007 to 2040.

Comment 1

Comment 2

(2)

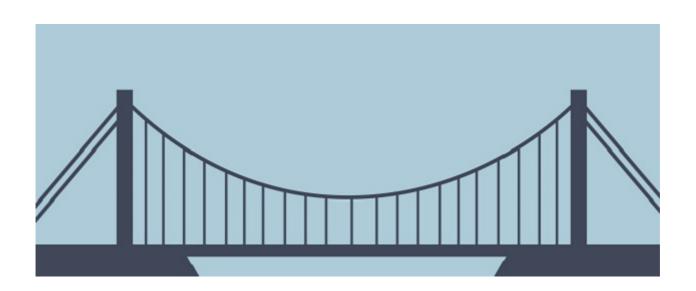
[3]

(Total 5 marks)



The Bridge to A level

Problem Solving





1 Solving quadratic equations

Question 1

A number and its reciprocal add up to $\frac{26}{5}$. Form and solve an equation to calculate the number.

(3)

Question 2

The diagram shows a trapezium.

Diagram **NOT** accurately drawn x + 3netres. x + 3 x + 3 x + 3 x + 3 x + 3 x + 3 x + 3 x + 3 x + 3 x + 3 x + 3

All the measurements are in centimetres. The area of the trapezium is 16 cm^2 .

- a) Show that $2x^2 + 5x 16 = 0$
- b) Work out the value of x to 1 decimal place.

(1)

Question 3

Two numbers have a product of 44 and a mean of 7.5. Use an algebraic method to find the numbers. You must show all of your working.

									(,	4	Ļ)	



Changing the subject 2

Question 1

The surface gravity of a planet is given by $g = \frac{GM}{r^2}$ where

M = Mass of the planet r = radius of the planet G = gravitational constant = $6.67x10^{-11}$

The surface gravity of Earth is $9.807 \,\mathrm{m/s^2}$ and the mass of Earth is $5.98 \times 10^{24} \mathrm{kg}$.

Find the radius of Earth in kilometres correct to 3 significant figures.

Question 2

In a parallel circuit, the total resistance is given by the formula $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$

Make R_1 the subject of the formula

(4)

(4)

Question 3

Show that $\frac{1}{\frac{1}{x}+1} = \frac{x}{x+1}$

(2)



3 <u>Simultaneous equations</u>

	(5)
Total / 10	

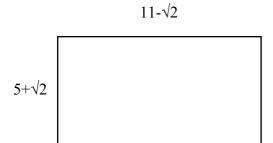


4 <u>Surds</u>

Question 1

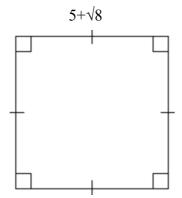
Calculate the area of each shape giving your answers in the form $a+b\sqrt{2}$

a)



(2)

b)



(3)

Question 2

Colin has made several mistakes in his 'simplifying surds' homework. Explain his error and give the correct answer.

i)
$$4\sqrt{3} \times 5\sqrt{12} = 20\sqrt{36}$$



Total / 10

Question 3

The area of a triangle is 20 cm 3 . The length of the base is $\sqrt{8}$ cm. Work out the perpendicular heign your answer as a surd in its simplest form.	ght givi	ing	
		(3	3)



5 <u>Indices</u>

Question 1

Lowenna says that $27^{-1/3} \times 64^{2/3} = 48$

Is Lowenna correct? You must show all of your working.

(4)

Question 2

Which one of these indices is the odd one out? Circle your answer and give reasons for your choice.

 $16^{-\frac{1}{4}}$

 $64^{-\frac{1}{2}}$

 $8^{-\frac{1}{3}}$

(2)

Question 3

Find values for a and b that make this equation work

$$a^{\frac{1}{2}} = b^{\frac{1}{3}}$$

(1)

Question 4

i) Write 25 as a power of 125

(1)

ii) Write 4 as a power of 32

(1)

iii) Write 81 as a power of 27

(1)



6 Properties of Lines

Question 1

- (a) Write down the gradient of the line 2y 4x = 5.
- (b) Write down the equation of a line parallel to 3y = 7 4x.

(1)

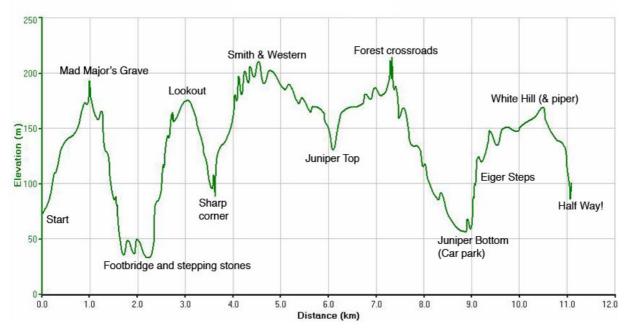
(1)

(c) Write down the equation of a line with gradient ½ and y-intercept of 6.

(1)

Question 2

Here is the profile of the first half of a fell running race.



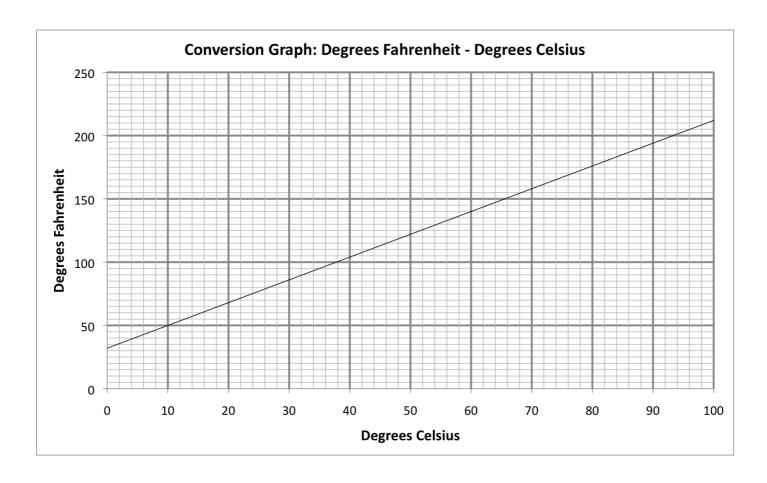
(a) Work out the approximate gradient of the race from the start to Mad Major's Grave

- (2)
- (b) The most dangerous part of the race is from Mad Major's Grave to the Footbridge. Why do you think this might be?
 - (1)
- (c) Work out an estimate for the average ascent for the first four uphill sections of the race.



Question 3

Here is a graph used to convert degrees Celsius (C) and degrees Fahrenheit (F).



The equation of the straight line is given by F = mC + aCalculate the values of m and a

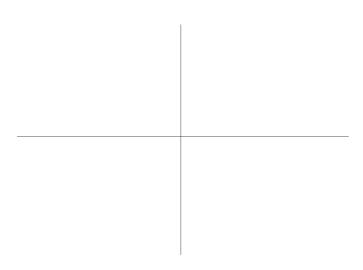
(2)



7 <u>Sketching curves</u>

Question 1

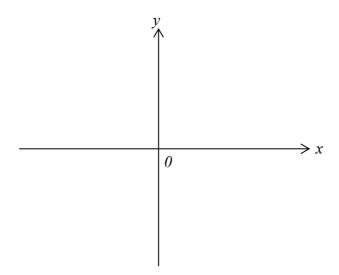
Sketch the graph of $f(x) = x^2 + 5x - 6$, showing the co-ordinates of the turning point and the coordinates of any intercepts with the coordinate axes.



(5)

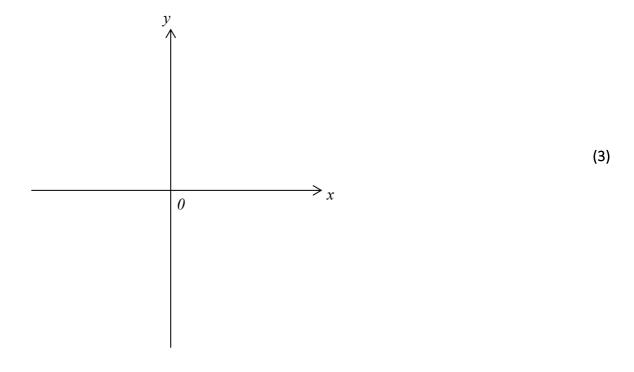
Question 2

a) On the axes sketch the graph of $y = \frac{3}{x}$ showing the coordinates of the turning point and the coordinates of any intercepts with the coordinate axes.





b) On the axes sketch the graph of $y = x^3 - 5$ showing the coordinates of the turning point and the coordinates of any intercepts with the coordinate axes.





8 <u>Transformation of functions</u>

Question 1

Here is a sketch of f(x).

The coordinates of P are (0,-2)

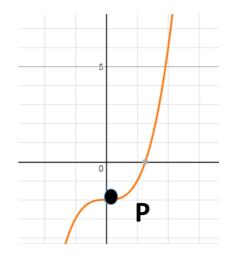
Sketch the graphs after the following translations and reflections, and state the coordinates of P':

a)
$$g(x) = f(x) + 1$$

b)
$$h(x) = f(x - 2)$$

c)
$$j(x) = -f(x)$$

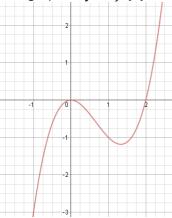
d)
$$k(x) = f(-x)$$



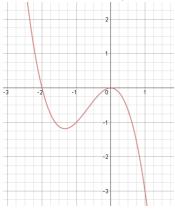
(4)

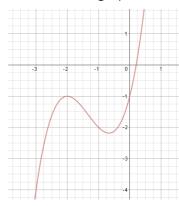
Question 2

The graph of y = f(x) is shown below.



Below each sketch, write down the equation of the transformed graph







Question 3

The equation of a curve is y = f(x) where $f(x) = x^2 - 4x + 5$ C is the minimum point of the curve. (a) Find the coordinates of C after the transformation f(x + 1) + 2.

(.....) **(2)**

(b) Hence, or otherwise, determine if f(x-3)-1=0 has any real roots. Give reasons for your answer.

(2)



9 <u>Pythagoras' theorem and Trigonometric ratios</u>

Question 1

ABCDEFGH is a cuboid

AE = 5cm

AB = 6cm

BC = 9cm

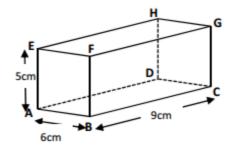


Diagram NOT drawn accurately

(a)	Calculate the leng	th of AG. Give	vour answer corr	ect to 3 significant fig	ures.
١	· ,	04.104.14.10				

(1)

(b) Calculate the size of the angle between AG and the face ABCD. Give your answer correct to 1 decimal place.

(3)

Question 2

A piece of land is the shape of an isosceles triangle with sides 7.5m, 7.5m and 11m.

Turf can be bought for £11.99 per 5m² roll.

How much will it cost to turf the piece of land?

2m B 2.2m

Question 3

Ben is 1.62m tall.

The tent he is considering buying is a square based pyramid.

The length of the base is 3.2m.

The poles AE, CE, AE and BE are 2m long.

Ben wants to know if he will be able to stand up in the middle of the tent. Explain your answer clearly.

.....

(3)



Sine / Cosine Rule 10

Question 1
Plane A is flying directly toward the airport which is 20 miles away. The pilot notice a second plane, B, 45° to her right. Plane B is also flying directly towards the airport. The pilot of plane B calculates that plane A is 50° to his left. Based on that information how far is plane B from the airport? Give your answer to 3 significant figures.
(4)
Question 2
Two ships, A and B, leave the same port at the same time. Ship A travels at 35km/h on a bearing of 130°. Ship B travels at 25km/h on a bearing of 120°. Calculate how far apart the ships are after 1 hour. Give your answer correct to two decimal places.
(3)
Question 3
A farmer has a triangular field. He knows one side measures 450m and another 320m. The angle between these two sides measures 80°. The farmer wishes to use a fertiliser that costs £3.95 per container which covers 1500m². How much will it cost to use the fertiliser on this field?

(3)



11 <u>Inequalities</u>

Question 1

A new cylindrical tube of snacks is being designed so that its height is 3 times its radius and its volume must be less than 20 times its radius.

Create an inequality and find possible values for the radius.

(3)

Question 2

A base jumper is going to jump off a cliff that is 50m tall, the distance she travels downwards is given by the equation

 $d = 4.9t^2$ where t = time of flight

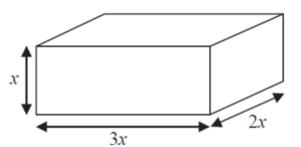
and d = distance travelled

A video camera is set-up to film her between 20m and 10m above the ground. Calculate the time period after the jumper jumps that filming taking place.

....(3)

Question 3

The total volume of the box is less than 1 litre. Given that all lengths are in cm and that x is an integer, Show that the longest side is less than 18cm.



(4)



12 <u>Algebraic proof</u>

Question 1

Katie chooses a two-digit number, reverses the digits, and subtracts the smaller number from the larger.

For example

$$42 - 24 = 18$$

She tries several different numbers and finds the answer is never a prime number.

Prove that Katie can never get an answer that is a prime number.

(4)

Question 2

Here are the first 5 terms of an arithmetic sequence

1 6 11 16 21

Prove that the difference between the squares of any 2 terms is always a multiple of 5.

(6)



13 Vectors

Question 1

OAB is a triangle

$$\overrightarrow{OA} = \mathbf{a} \text{ and } \overrightarrow{OB} = \mathbf{b}$$

(a) Find the vector AB in terms of **a** and **b**

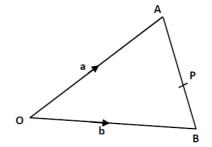


Diagram NOT drawn accurately

(1)

P is the point on \overrightarrow{AB} such that AP: PB = 3:2

(b) Show that $\overrightarrow{OP} = \frac{1}{5} (2\mathbf{a} + 3\mathbf{b})$

.....(3)

Question 2

OABC is a parallelogram.

X is the midpoint of OB

$$\overrightarrow{OA} = \mathbf{a} \text{ and } \overrightarrow{OC} = \mathbf{c}$$

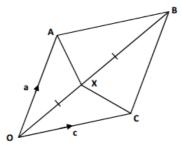


Diagram NOT drawn accurately

(a) Find the vector \overrightarrow{OX} in terms of **a** and **c**.

(1)

(b) Find the vector XC in terms of **a** and **c**.



Question 3

PQRS is a parallelogram. M is the midpoint of RS N is the midpoint of QR

$$\overrightarrow{PQ} = 2\mathbf{a}$$

$$\overrightarrow{PS} = 2\mathbf{b}$$

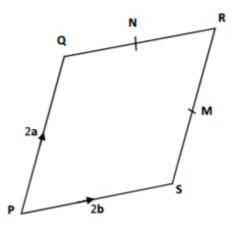


Diagram NOT drawn accurately

Use vectors to proof that the line segments SQ and MN are parallel.

(3)



14 <u>Probability</u>

Question 1

Max has an empty box.

He puts some red counters and some blue counters into the box.

The ratio of the number of red counters to the number of blue counters is 1:3.

Julie takes at random 2 counters from the box.

The probability that she takes 2 red counters is $\frac{19}{316}$.

How many red counters did Max put in the box?

(5)



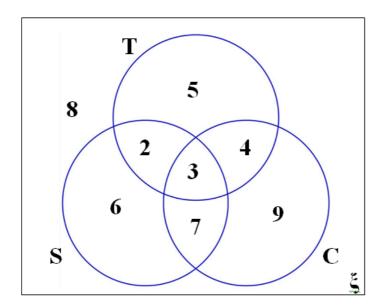
(2)

Question 2

The Venn diagram shows the ice-cream flavours chosen by a group of 44 children at a party.

The choices are strawberry (S), choc-chip (C) and toffee (T).

A child is picked at random.



Work out:
(a) P(S)

(1)
(b) P(T U C | C)

(c) P(C | S U T)

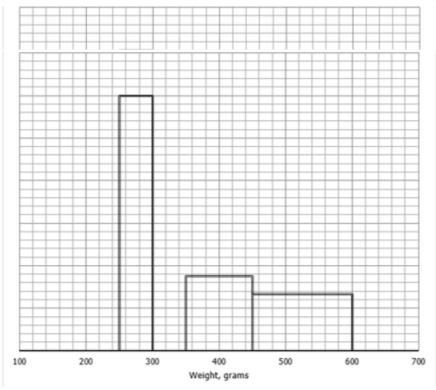


15 <u>Statistics</u>

Question 1

The table and histogram show the weights of some snakes.

W	eight, gr	Frequency	
250	< x <	300	60
300	< x ≤	325	25
325	< x ≤	350	40
350	< x <	450	35
450	< x ≤	600	40
		Total	200



- (a) Use the information to complete the histogram
- (b) Calculate an estimate for the median

(3)

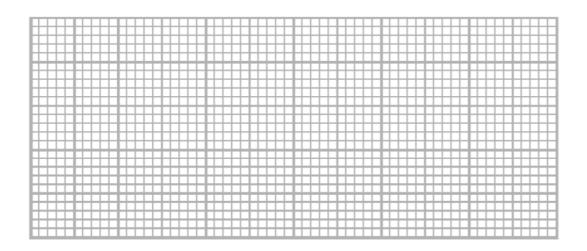
.....



Question 2

Sarah played 15 games of netball. Here are the number of goals she scored in each game.

a) Draw a boxplot to show this information



a) Lucy plays in the same 15 games of netball. The median number of points Lucy scores is 24. The interquartile range of these points is 10 and the range of these points is 17.

Who is the better player, Sarah or Lucy? You must give a reason for your answer.

(2)

(3)